Energy partition in two solar flare/CME events

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- [1] Using coordinated observations from instruments on the Advanced Composition 6
- Explorer (ACE), the Solar and Heliospheric Observatory (SOHO), and the Ramaty High 7
- Energy Solar Spectroscopic Imager (RHESSI), we have evaluated the energetics of 8
- two well-observed flare/CME events on 21 April 2002 and 23 July 2002. For each event, 9
- we have estimated the energy contents (and the likely uncertainties) of (1) the coronal
- mass ejection, (2) the thermal plasma at the Sun, (3) the hard X-ray producing accelerated 11
- electrons, (4) the gamma-ray producing ions, and (5) the solar energetic particles. The 12
- results are assimilated and discussed relative to the probable amount of nonpotential 13
- magnetic energy available in a large active region. INDEX TERMS: 7519 Solar Physics, 14
- Astrophysics, and Astronomy: Flares; 7513 Solar Physics, Astrophysics, and Astronomy: Coronal mass 15
- ejections; 7514 Solar Physics, Astrophysics, and Astronomy: Energetic particles (2114); 7554 Solar Physics,
- 17 Astrophysics, and Astronomy: X rays, gamma rays, and neutrinos; KEYWORDS: solar flares, coronal mass
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Introduction

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[2] Solar flares and coronal mass ejections (CMEs) are the most powerful events in the solar system. In tens of minutes they can convert in excess of 10^{32} ergs of magnetic energy into accelerated particles, heated plasma, and ejected solar material. While the order of magnitude of this total energy is not in serious doubt, its partition amongst the component parts of the flare and CME has yet to be reliably evaluated for a particular event or set of events. A reliable estimate of this partition, and of its variation from event to

event would provide powerful constraints on the energy 33 release process(es) at work.

[3] Various previous studies have examined the energy 35 budget of a limited number of energy components in certain 36 flares. For example, Canfield et al. [1980] evaluated the 37 radiative energy budget of a solar flare on 5 February 1973. 38 However, without the benefit of hard X-ray or gamma-ray 39 observations, they were not able to make an assessment of 40 the role of energetic particles in the event. Neither were they 41 able to assess the kinetic energy in the confined flare 42 plasma, in any associated coronal mass ejection, or in 43 accelerated interplanetary particles. Strong et al. [1984] 44 assessed the energy contents in thermal plasma, nonthermal 45 electrons, and hydrodynamic mass motions of nonejected 46 material for two flares within the same active region on 31 47 August 1980. Most recently, Saint-Hilaire and Benz [2002] 48 presented an energy budget for a compact flare that oc- 49 curred on 20 February 2002. They included the thermal and 50 radiative energy of the flare plasma, the nonthermal electron 51 beam energy, and the kinetic energy of the non-CME- 52 associated plasma ejecta. Neither of these latter studies, 53 however, were able to include an assessment of the energy 54 content in accelerated ions, nor did they attempt an evalu- 55 ation of the energies in the CME, interplanetary shock, or 56 accelerated interplanetary particles.

[4] Our observational database with which to address 58 questions of flare/CME energetics has steadily improved 59 over time, to the point where a more comprehensive 60 assessment of the energy content of various components 61 of the flare is now possible. For example, observations of 62 CMEs are available on a continuous duty cycle from the 63 LASCO instrument on the SOHO spacecraft. Estimates of 64

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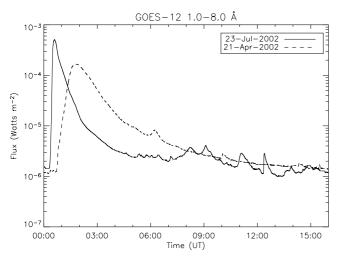


Figure 1. GOES 1-8 Å light curves for the two events studied. The zero of the time axis coincides with 0000 UT on each date.

the energy in accelerated charged particles and in the flare thermal plasma can be made through interpretation of the X-ray and gamma ray signatures observed by the Ramaty High Energy Solar Spectroscopic Imager (RHESSI). Finally, the Advanced Composition Explorer (ACE) suite of instruments provides information on the energy in accelerated interplanetary particles.

- [5] From 7 to 9 October 2003 a workshop was held in Taos, New Mexico to investigate problems of common interest to investigators working on data from the ACE, RHESSI, and Wind missions. Working Group 5 at that workshop addressed the task of evaluating the energetics of the various components in two well-observed flare/CME events, a GOES X1.5 flare on 21 April 2002 and an X4.8 event on 23 July 2002; this paper is the result of that collaboration.
- [6] Figure 1 shows the GOES soft X-ray light curves for the two events studied. The 21 April event was a long-lived soft X-ray event, with significant 1–8 Å flux observable over 12 hours after the flare onset; it occurred near the west limb at S14W84. Its overall properties have been discussed by *Gallagher et al.* [2002]. By contrast, the 23 July event was much more impulsive, was a strong emitter of hard X rays and gamma rays [see *Lin et al.*, 2003], and was located near the east limb at S13E72.
- [7] In section 2 we consider the energetics of the CMEs associated with these events. In section 3 we evaluate the energetics of the hot, soft X-ray emitting plasma produced during the flare and that of hard X-ray producing accelerated electrons. In section 4 we turn our attention to the energetics of accelerated ions. In section 5 we consider the energetics of the interplanetary particles commonly believed to have been accelerated by the CME-associated shock. In section 6 we consider the available energy in stressed magnetic fields. In section 7 we summarize the results in tabular form and discuss their significance.

101 2. CME Energetics

[8] Coronal mass ejections for both the 21 April 2002 and 23 July 2002 events were well observed by both the

LASCO C2 and C3 coronagraphs [Brueckner et al., 1995] 104 on SOHO [Domingo et al., 1995] (Figure 2). A detailed 105 analysis of the propagation of the 21 April CME through the 106 corona as observed by TRACE, UVCS, and LASCO is 107 given by Gallagher et al. [2003].

- [9] With the use of calibrated LASCO images, we can 109 derive estimates of the kinetic and potential energy of the 110 two CMEs. The procedure is as follows: First, we select an 111 image containing the CME and a preevent image, as close in 112 time as possible to the flare, which does not show any 113 disturbances or ejecta over the path of the subsequent CME. 114 Next, the images are calibrated (in units of mean solar 115 brightness) and the preevent image is subtracted from the 116 CME image. The excess brightness revealed by this sub- 117 tracted image is due to Thompson scattering of photospheric 118 radiation from the excess mass in the CME.
- mass of the CME under the usual assumptions [Poland et 121 al., 1981; Vourlidas et al., 2000, 2002] as follows: (1) all of 122 the CME mass is concentrated on the plane of the sky, and 123 (2) the CME material consists of 90% H and 10% He. We 124 invoke the first assumption because the true three-dimensional distribution of the CME mass along the line of sight 126 is unknown. It is a very good assumption here, since both of 127 our CMEs originated from regions very close to the limb 128 and are very likely propagating along the sky plane. The 129 second assumption represents an "average" coronal composition since we do not know the height at which the bulk 131 of the CME material originates (other than that it is 132 coronal).
- [11] These assumptions together result in an uncertainty 134 about the true mass of a CME which becomes more 135 significant as the central angle and/or spread of a given 136 CME departs significantly from the sky plane. The mass 137 uncertainty is about a factor of 2 for CMEs that are 138 40 degrees from the sky plane [Vourlidas et al., 2000]. 139 Generally speaking, one should be aware of other uncertainties in this procedure that include exposure time 141 variations between event and preevent images, improper 142 vignetting correction, solar rotation effects, and the presence of stars in the field of view. Fortunately, such 144 uncertainties can be minimized to a level that is well 145 below that of other factors through proper calibration and 146 careful choice of event and preevent images, as we have 147 done here.
- [12] After obtaining a series of excess mass images of the 149 CME as a function of time, we can compute the total mass 150 of the CME and the position and projected velocity of both 151 the leading edge and the center of mass of the CME. From 152 the mass, projected velocity, and position data follow 153 estimates of the total kinetic $(U_{\rm K})$ and potential (U_{Φ}) 154 energies [Vourlidas et al., 2000]. Thus one can, in principle, 155 follow the evolution of the energy and mass as the CME 156 propagates outward in the corona. However, while this is 157 possible for the majority of LASCO CMEs, it is not the case 158 for the two events considered here, which both move very 159 quickly through the C2 field of view, leaving only the C3 160 images for analysis. Moreover, in the 21 April event, high 161 intensities of energetic particles reached the SoHO space- 162 craft within less than an hour of the flare peak; these 163 particles produced large numbers of solar particle hits on 164 the LASCO detectors, making later images unusable for 165

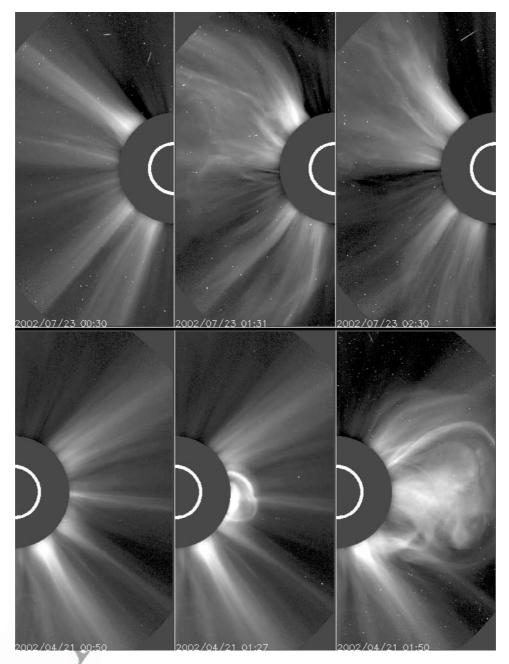


Figure 2. LASCO/C2 observations of the 23 July (top) and 21 April 2002 (bottom) flare/CME events. The configuration of the preevent corona is shown in the leftmost panels. The CMEs were very fast so only a couple of C2 images are available. The observation times are shown on the figures.

quantitative analysis. For these reasons, we are only able to provide mass and energy measurements from the LASCO/ C3 image that shows all (or at least most) of the event mass during the period when solar particle hits were not a significant factor.

[13] Table 1 shows the mass and the projected velocities 171 at $10R_{\odot}$ and $18R_{\odot}$, respectively, at 0218 UT for each event, 172 as well as estimates for the associated kinetic and potential 173 energies. Note that the 21 April event was an accelerating 174 event, and a second-order fit to the position data yields a 175

t1.1 Table 1. LASCO CME Measurements

t1.2	Event	Mass, 10 ¹⁵ g	Speed at $10R_{\odot}$, km s ⁻¹	Speed at $18R_{\odot}$, km s ⁻¹	Kinetic Energy U_K , 10^{30} erg	Potential Energy U_{Φ} , 10^{30} erg
t1.3	21 April 2002	2.8	2300	2700	180	4.6
t1.4	23 July 2002	7.1	2600	2000	110	12

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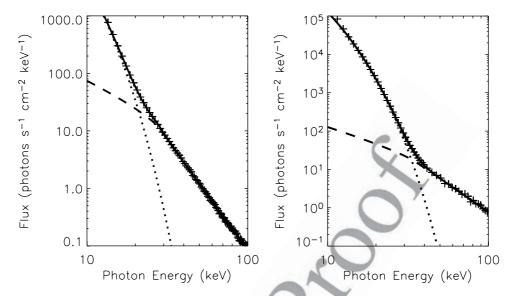


Figure 3. Sample RHESSI spectra and fits for the 21 April 2002 (left) and 23 July 2002 (right) flares. The plus signs denote the data points. The data were fit from 15 keV to 100 keV with the bremsstrahlung from an isothermal plasma (dotted curve) and the bremsstrahlung from a double-power-law mean electron flux distribution with a low-energy cutoff (dashed curve). The solid curve, the best-fit spectrum, is the sum of these two spectra. The time intervals are 0115:00–0116:00 UT for the 21 April spectrum and 0035:00–0036:00 UT for the 23 July spectrum.

mean acceleration of 156 m s⁻², two orders of magnitude larger than the solar gravitational acceleration at this distance. By contrast, the 23 July event first accelerates and then quickly decelerates in the LASCO/C3 field of view. Consequently, no single value provides an adequate characterization of the acceleration profile for this event.

[14] These results further reinforce our notion that these are unusual CME events. Their large kinetic energies place both of them in the top 1% of all observed CMEs for the period 1996–2000 [Vourlidas et al., 2002]. In both cases, the gravitational potential energy is only some 10% of the total energy contained in the CME. The uncertainties in these values are dominated by the uncertainty in the mass and are estimated to be a factor of ~2.

3. Energetics of the Thermal Plasma and Accelerated Electrons

[15] The energy content of both the hottest thermal plasma and the accelerated (nonthermal) electrons can be derived from the RHESSI X-ray images and spectra. We choose to treat these two components separately even though this results in some double budgeting, since the nonthermal electrons will contribute to the plasma heating as they lose their energy by Coulomb collisions. This is expected to be most significant when the Neupert Effect (after *Neupert* [1968]) is obvious from the light curves [*Dennis et al.*, 2003].

[16] In the impulsive phase of both flares studied here, a thermal component is clearly visible in the X-ray spectra at the lowest photon energies (Figure 3). A flatter extension to higher energies is interpreted as bremsstrahlung emission from a nonthermal electron beam in a thick target. We used a parametric isothermal plus a double power law function for the mean source electron spectrum $\bar{F}(E)$ [Brown et al.,

2003] in conjunction with the bremsstrahlung cross section 209 of Haug [1997] to fit the observed hard X-ray spectrum 210 [Holman et al., 2003]. The results presented here were 211 obtained from a sequence of $\bar{F}(E)$ spectra calculated for 212 contiguous 20-s intervals throughout each flare using X-ray 213 flux measurements above 10 keV, where the RHESSI 214 spectral response is best known.

3.1. Hot Plasma

[17] We have carried out an analysis of the thermal 217 plasma similar to that reported by Moore et al. [1980] and 218 Strong et al. [1986]. The energy going into plasma heating 219 during each flare was estimated by computing the time 220 evolution of the energy content of the thermal plasma and 221 obtaining the peak value. This constitutes a lower limit to 222 the thermal energy, since it does not account for the cooling 223 of the plasma prior to this time nor to any heating at later 224 times. Each of these additional contributions are considered 225 separately below; they are believed to add perhaps a factor 226 of 3 to the peak thermal energy. No attempt was made to 227 determine the kinetic energy of turbulent and directed 228 plasma motions, since no spectrally resolved lines were 229 available to give a measure of line broadening caused by 230 such bulk motions. For other flares observed with the Bragg 231 Crystal Spectrometers on SMM and Yohkoh, the energy in 232 this component has generally been estimated to be a small 233 fraction of the thermal energy in the plasma [Strong et al., 234 1986].

[18] The thermal energy of the heated plasma was 236 obtained from the temperature T_0 (K) and emission measure 237 $EM = \int_V n_e^2 dV \, (\text{cm}^{-3})$ for the thermal portion of the spectral 238 fit. Here n_e is the electron density (cm⁻³) and V is the 239 emitting volume (cm³). Account must be taken of the filling 240 factor f equal to the ratio of the emitting volume to the 241 apparent volume (V_{ap}) as determined with an imaging 242

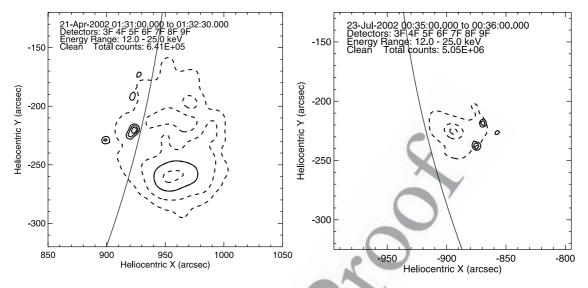


Figure 4. RHESSI images for (left) the flare on 21 April 2002 at 0131:00–0132:30 UT and (right) the flare on 23 July 2002 at 0035:00–0036:00 UT. Both images were obtained using the CLEAN reconstruction algorithm. They correspond to the time of peak soft X-ray emission when all the shutters were in the RHESSI detector fields of view for both events. The 12–25 keV contours are labeled as follows: (left) 10% (broken), 20% (broken), 50% (solid), and 90% (broken); (right) 20%, 50%, and 90% (all broken). The 30–100 keV contours are solid in both images and correspond to 40, 60, and 80% of peak value. The curved line shows the solar limb in each image.

instrument having limited spatial resolution. The thermal energy content of the plasma is then given by the following expression [e.g., *de Jager et al.*, 1986]:

$$U_{\rm th} = 3 \, n_e \, k T_0 \, f \, V_{\rm ap} \simeq \, 4.14 \times 10^{-16} \, T_0 \, \sqrt{EM \times f \, V_{\rm ap}} \, {\rm erg}, \ \ (1)$$

where k is Boltzmann's constant.

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[19] We estimated the source volume from the area information obtained from the RHESSI observations. However, it is nontrivial to determine the area of a source from the RHESSI measurements of the modulated flux with its nine collimators with different spatial scales. We have used the technique for doing this for a single symmetrical source described by Schmahl and Hurford [2002]. In this technique the modulation amplitude is determined for each of the collimators and the rotationally averaged size determined that would give that distribution of values. For the 21 April flare at 0131 UT, the FWHM of the 12-25 keV source determined in this way was 26 arcsec, giving a source area of $\pi \times (13)^2 = 530 \text{ arcsec}^2$. This is consistent with the area of the 50% contour of the 12-25 keV image shown in Figure 4 that was produced from the RHESSI data using the CLEAN reconstruction algorithm [Hurford et al., 2002].

[20] This image and the distribution of modulation amplitudes both show that a more extended source was also present with a factor of \sim 10 smaller brightness extending out to sizes possibly as large as 180 arcsec, the largest source that will still produce modulation through RHESSI's coarsest collimators. Its location and extent match the emission seen in the TRACE images at the same time. From the 12–25 keV image shown in Figure 4, we estimate that the area of the extended source was 3×10^4 arcsec² and that it produced approximately 1/3 of the total emission.

Hence it must have contained twice as much thermal energy 275 as the compact source. 276

[21] For the 23 July 2002 flare between 0035 and 277 0036 UT, the *Schmahl and Hurford* [2002] method gives 278 a source FWHM of 16 arcsec, a value matched by the area 279 within the 50% contour of the 12–25 keV image shown in 280 Figure 4. In this case, no significant extended source is 281 evident in the distribution of modulation amplitudes or in 282 the reconstructed image.

[22] We estimated the source volumes from the areas A 284 (cm²) discussed above assuming $V_{\rm ap} = A^{3/2}$ and a filling 285 factor of unity (f=1). Aschwanden and Parnell [2002] 286 have suggested, based on their fractal analysis of flare 287 geometry, that the relation $V_{\rm ap} = A^{1.3\pm0.1}$ may be a better 288 way to determine the flare volume from the measured area. 289 However, for the large flares considered here, this empirical formula results in unreasonable density estimates 291 (as high as 10^{13} cm⁻³) and so we have not used this 292 expression.

[23] Application of equation (1) to the 21 April and 23 294 July events yields values of $U_{\rm th}=1.3\times10^{31}$ ergs 295 (including the extended source) and 7×10^{30} ergs, 296 respectively. Since both EM and T_0 are well determined 297 observationally, the principal uncertainties in these values 298 arise from uncertainties in the filling factor f and the 299 apparent volume $V_{\rm ap}$. From equation (1) and the relation 300 $V_{\rm ap}=A^{3/2}$, we may write

$$\Delta \log U_{\text{th}} = \sqrt{\left(\frac{1}{2}\Delta \log f\right)^2 + \left(\frac{3}{4}\Delta \log A\right)^2}.$$
 (2)

With an estimate of $\Delta \log A = \pm 0.5$ and $\Delta \log f = [+0, -2]$ 303 (a filling factor between 1% and unity), we obtain $\Delta \log$ 304 $U_{\rm th} = [+0.4, -1]$.

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[24] More sophisticated fits using a differential emission measure distribution with temperature $DEM(T) \equiv n_e^2 dV/dT$ (e.g., $\propto T^{-\alpha}$) will be used in future work as the RHESSI spectral analysis becomes more capable and our knowledge of the instrument response matrix improves in the different attenuator states. Also, extending the spectral fits to energies below 10 keV, down to RHESSI's lower limit near 3 keV, will provide better estimates of the thermal spectrum at lower temperatures. This will allow the exploitation of the iron and nickel line complexes at \sim 6.7 keV and \sim 8 keV that can be measured with RHESSI's \sim 1 keV FWHM energy resolution [*Phillips*, 2004].

[25] An estimate of the energy in the hot flare plasma can also be obtained from GOES soft X-ray data. The GOES instruments provide X-ray fluxes in two broad bands, 1.6–12 keV and 3–25 keV. The ratio of the fluxes in these bands and the X-ray intensity provide an estimate of the flare temperature and emission measure, respectively. The thermal energy can then be estimated from equation (1). Since the hard X-ray energies observed with the GOES detectors are lower than the lowest energies observed with RHESSI, the GOES detectors tend to be sensitive to somewhat lower temperature plasma than RHESSI. When RHESSI spectral fits indicated a temperature of 37 MK for the 23 July flare, for example, the temperature deduced from the GOES data was 27 MK. The peak thermal energies deduced from the GOES results for the 21 April and 23 July flares were 1×10^{31} erg in both cases, i.e., comparable to the values obtained with

[26] In addition to the peak energy content of the thermal plasma, a comprehensive assessment of the thermal energy must also include estimates of the energy losses by conduction and radiation during the flare and of any additional energy release during the decay phase of the flare. Conductive cooling is difficult to estimate since, during the impulsive phase at least, a collision-dominated conduction expression is probably not valid [see, e.g., Smith and Lilliequist, 1979]. A. M. Veronig et al. (The Neupert effect: A comparison of data and theory using RHESSI and GOES observations, submitted to Astrophysics Journal, 2004, hereinafter referred to as Veronig et al., submitted manuscript, 2004) however, suggest that conductive cooling can result in an energy loss for other flares that is greater than the peak thermal energy content of the plasma. However, for the flares considered here, the simple model they assume is not applicable given the obvious complexity of the magnetic field and the involvement of multiple loop structures. Future work using the multiple loop modeling done by Reeves and Warren [2002] may be able to make realistic estimates of the conductive cooling term, at least for the decay phases of these flares.

[27] Radiative losses are much easier to estimate since they depend only on the emission measure, temperature, and composition of the emitting plasma. We have estimated their magnitude using the standard radiative loss function in the Chianti code, assuming coronal abundances. Assuming that radiation was the only cooling mechanism, the additional energy required to maintain the plasma with the measured emission measure and temperature during the

decay phase of the flare was estimated from the GOES data 368 and found to be 1.8×10^{31} ergs for the 21 April 2002 flare 369 and 1.3×10^{31} ergs for the 23 July 2002 flare. 370

3.2. Accelerated Electrons

[28] The energy in accelerated electrons was determined 372 from the power law extension to the measured X-ray 373 spectrum assuming a thick target model. In this model the 374 accelerated electrons ultimately lose all of their suprathermal 375 energy through collisions with ambient thermal electrons. 376 The injected electron energy spectrum $F_0(E_0)$ (electrons 377 cm⁻² s⁻¹ keV⁻¹) required to produce the inferred mean 378 source spectrum $\bar{F}(E)$ in a collisional cold target is [Brown 379 and Emslie, 1988]

$$F_0(E_0) = \frac{K}{A_i} \left(\frac{\bar{F}(E)}{E^2} \left[1 - \frac{d \ln \bar{F}}{d \ln E} \right] \right)_{E=E_0}, \tag{3}$$

where A_i is the electron injection area (cm²) and $K = 2\pi e^4 \Lambda$, 382 e being the electronic charge and Λ the Coulomb logarithm 383 appropriate to the ionization state of the target (see below). 384 The corresponding injected energy (ergs) is

$$U_{e} = A_{i} \int_{t} \int_{E_{min}}^{\infty} E_{0} F_{0}(E_{0}) dE_{0} dt$$

$$= K \int_{t} \int_{E_{min}}^{\infty} \frac{\bar{F}(E_{0})}{E_{0}} \left[1 - \frac{d \ln \bar{F}(E_{0})}{d \ln E_{0}} \right] dE_{0} dt. \tag{4}$$

Note that the value of the injection area A_i cancels between 387 equations (3) and (4); the electron energy is determined 388 from the time integral of the total hard X-ray flux without 389 the need to assume a value for A_i . Also, the accumulated 390 energy, obtained by integrating the calculated injected 391 electron power over time, was in practice calculated by 392 summing over all the discrete 20-s time intervals for which 393 spectra were obtained.

[29] The above equations assume a cold target in the 395 sense that the thermal electrons have a mean energy (kT) 396 that is significantly lower than the lowest energy of the 397 nonthermal beam electrons. In addition, consideration must 398 be given to the ionization state of the target since the 399 bremsstrahlung efficiency (ergs of hard X rays produced 400 per erg of injected electron energy) is a factor of ~3 times 401 lower for a fully ionized plasma than for a neutral target, a 402 consequence of the reduced Coulomb logarithm, and so 403 lower collisional loss rate, appropriate [Brown, 1973; 404 Emslie, 1978]. Since most of the beam energy is in the 405 lower-energy electrons that stop higher in the corona, we 406 used a Coulomb logarithm parameter appropriate for a fully 407 ionized plasma to calculate the total nonthermal energy. A 408 more refined calculation is possible using the procedure 409 outlined by Kontar et al. [2002], but no significant differ- 410 ence is expected in the result.

[30] In our analysis we used a form $F_0(E_0) \propto E_0^{-\alpha}$ between 412 a low-energy cutoff, $E_{\rm min}$, and a break energy, $E_{\rm brk}$, and 413 $F_0(E_0) \propto E_0^{-\beta}$ above $E_{\rm brk}$. For the 21 April flare, only a 414 single power law index, α , was required to fit the X-ray 415 data. In the thick target model, this results in an X-ray 416 spectrum of the form $I(\epsilon) \propto \epsilon^{-\gamma}$ above $\epsilon_{\rm min} = E_{\rm min}$, where ϵ 417 is the X-ray photon energy and $\gamma = \alpha - 1$. The X-ray 418 spectrum flattens below $\epsilon_{\rm min}$ [see Holman, 2003]. The full 419

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double power law fit was required for the 23 July flare. The photon spectrum below $E_{\rm brk}$ is steeper than $\alpha-1$ because of the reduced number of electrons above $E_{\rm brk}$ [Holman, 2003].

[31] The calculated values of α for the 21 April flare range from 4.5 to 8.5, and for the 23 July flare α ranges from 2 to 8 and β ranges from 4 to 9 [e.g., Holman et al., 2003]. Because of the steep form of these electron distributions, the value of U_e is particularly sensitive to the lower cutoff value E_{\min} in equation (4). However, since thermal emission dominates the low-energy part of the photon spectrum as discussed above, the value of E_{\min} cannot be directly determined. E_{\min} can, in principle, be determined using RHESSI's imaging spectroscopy. By obtaining spectra of nonthermal X-ray sources that are spatially separated from the thermal sources, the nonthermal spectrum should be independently determined without thermal contamination. However, the RHESSI images herein have a limited dynamic range of \sim 10:1 because of the Fourier imaging technique that is used and uncertainties in the knowledge of the grid modulation characteristics; the dynamic range will improve as these characteristics are better determined. This limitation and the steepness of the spectra prevent the nonthermal sources from being visible at energies much below the energy at which the steep thermal spectrum begins to dominate. Therefore we could not deduce the value of the low-energy cutoffs from the imaged spectra.

[32] Since the thermal spectrum is so dominant at low energies, the nonthermal power-law part of the electron spectrum can be extended down to arbitrarily low energies while still maintaining an acceptable fit to the overall spectrum. We therefore chose the largest value of $E_{\rm min}$ that still gave an acceptable fit (normalized $\chi^2 \simeq 1$) to the spatially integrated spectral data; as a result, the energies we obtain are necessarily lower limits to the energy in the nonthermal electrons. This is in contrast to previous work where a constant energy is chosen for the value of the lowenergy cutoff (for example, *Saint-Hilaire and Benz* [2002] fixed the low-energy cutoff at 10 keV).

[33] Early in the 23 July flare, before the impulsive rise, there was no obvious transition from predominantly thermal (i.e., steep, concave downward in log-log space) to predominantly nonthermal (i.e., shallow, near straight line in log-log space) forms of photon spectra. This is often the case early in a flare. Instead, we found that the data could be fitted with double power law photon spectra alone and therefore were consistent with pure nonthermal emission. However, this led to unreasonably high energy contents very early in the preimpulsive phase [Holman et al., 2003]. The combination of an isothermal spectrum and a double power law with a low-energy cutoff provides an equally good fit to the data. Thus in keeping with the philosophy of minimizing the energy in nonthermal electrons, the data were fitted with this combined isothermal/nonthermal model. (An alternative possibility, that this early emission was multithermal, will also be considered once the RHESSI spectral analysis is developed to allow fluxes below 10 keV to be reliably included in the fits.) Values of E_{\min} ranged from a low of 18 keV to a high of 75 keV [see Holman et al., 2003]. Throughout most of the event, E_{\min} ranged from 20 to 40 keV.

[34] Veronig et al. (submitted manuscript, 2004) have 482 calculated the value of $E_{\rm min}$ based on the energy required 483 to produce the observed soft X-ray plasma, through a 484 generalization of the analysis of the Neupert Effect. Values 485 of $E_{\rm min}$ determined by this method, applied to four other 486 flares in April 2002, lie in the range 15–30 keV, consistent 487 with our findings.

[35] For the 23 July event, the electron energy deter-489 mined by this method was found to be $U_{\rm e}=3\times10^{31}$ erg. 490 The result for the 21 April event was $U_{\rm e}=2\times10^{31}$ erg. 491 Despite uncertainties (which we estimate are approximately half an order of magnitude, originating mainly in 493 the determination of $E_{\rm min}$), these results are, somewhat 494 surprisingly, higher than the corresponding values of 1.3×495 10^{31} erg and 7×10^{30} erg for the energy contained in the 496 thermal plasma $U_{\rm th}$. This surprising result is reinforced by 497 the the wide lower error bar on $U_{\rm th}$ caused by the 498 uncertain filling factor f and the fact that U_e may be an 499 underestimate. It will be interesting to see if this result 500 holds for other flares.

4. Energetics of Accelerated Ions

[36] Accelerated ions are energetically important in large 504 solar flares with significant emission above ~300 keV 505 [Ramaty and Mandzhavidze, 2000]. They manifest them- 506 selves principally through the production of gamma-ray 507 lines in the range $\sim 1-10$ MeV [e.g., Ramaty et al., 508 1979]. We plot the time-integrated γ -ray count spectrum 509 of the 23 July 2002 flare in Figure 5, along with the best 510 overall fit and the best-fitting bremsstrahlung and total 511 nuclear components. The nuclear component is composed 512 of moderately broadened lines produced by p and α 513 reactions on ambient C, O, Ne, etc., and highly broadened 514 lines from accelerated C, O, Ne, etc., ion reactions on 515 ambient H and He (an unresolved nuclear continuum 516 merges with this broad component). The flux in the highly 517 broadened component is typically $>3\times$ that in the moder- 518 ately broadened component.

[37] Since nuclear states producing spectral lines have 520 different excitation thresholds, the ratio of line intensities 521 provides information on the ratio of ion fluxes at different 522 energies, i.e., on the shape of the accelerated ion spectrum. 523 There is a small dependence on the angular distribution of 524 accelerated ions that pales in comparison with the uncerstainty in spectral shape. For the 23 July flare we used 526 intensities of the moderately Doppler-broadened 12 C 527 (4.43 MeV) deexcitation line, the total nuclear deexcitation 528 line complex from 4 to 7 MeV, and the neutron-capture line 529 at 2.223 MeV. Assuming an ion spectrum of the form F(E) 530 $\sim E^{-\beta}$, we found that β ranged between \sim 3.5 and 4.5 [*Lin et* 531 *al.*, 2003].

[38] Because the threshold energies for producing these 533 nuclear lines are ≥ 2.5 MeV, the spectrum below that energy 534 is unknown. In estimating the energy in accelerated ions, we 535 normalize to the nuclear fluence in the 4–7 MeV range, 536 (163 ± 14) γ cm⁻² [*Lin et al.*, 2003]. Assuming that the ion 537 spectrum continues unbroken down to 2.5 MeV Nucleon⁻¹ 538 and is flat below that energy, we estimate that the flare-539 accelerated protons contained (1.0–4.0) \times 10³⁰ ergs of 540 energy. This is likely to be a lower limit to the energy in 541 protons; e.g., if the proton spectrum were to continue down 542

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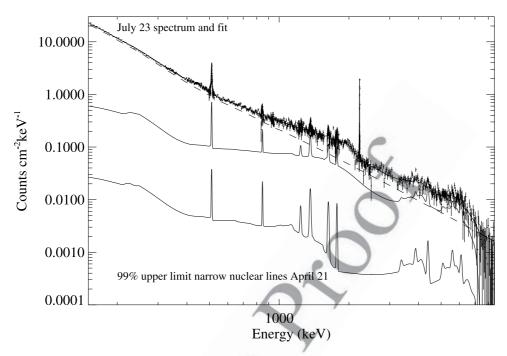


Figure 5. Spectrum of the 23 July flare with the best fit overplotted. The dashed curve is the bremsstrahlung component; the solid curve is the total nuclear component. The 99% confidence limit on the moderately broadened nuclear line component for the 21 April flare is shown for comparison.

to 1 MeV without a break, the energy contained in protons would increase to $(4-40) \times 10^{30}$ ergs; if the power law extended down to 0.1 MeV, this energy would increase to $(1.2-120) \times 10^{32}$ ergs. Under the further assumption of "impulsive flare" abundances [*Ramaty et al.*, 1996] and with accelerated $\alpha/p = 0.5$, $\alpha/O = 50$, and $^3\text{He}/^4\text{He} = 1$, we can estimate the total energy content in protons and heavier ions. For a power law spectrum unbroken down to 2.5 MeV Nucleon⁻¹ and flat below that energy, that energy is $U_i \simeq (6-24) \times 10^{30}$ ergs. For a power law spectrum unbroken down to 1 MeV Nucleon⁻¹ that energy is $U_i \simeq (2.4-24) \times 10^{31}$ ergs; for a low-energy cutoff of 0.1 MeV Nucleon⁻¹ it is $U_i \simeq (7-700) \times 10^{32}$ ergs.

[39] No significant y-ray line emission was produced in the 21 April 2002 flare; bremsstrahlung emission during that event was only observed up to \sim 350 keV. We have obtained an upper limit on the energy in accelerated ions during the flare by fitting the γ -ray count spectrum with a nuclear-line template and a power law bremsstrahlung component. In order to reduce systematic effects due to background, we have only used our fit to the moderately broadened nuclear deexcitation lines in our determination of the upper limit to the energy. We plot our fit to this component in Figure 5 relative to the total nuclear component fit to the 23 July flare. From this fit we obtain a 99% confidence upper limit of 3.7 γ cm⁻² on the fluence in the moderately broadened 4.439 MeV 12 C line. Under the assumption that the power law index of accelerated ions was 4.5 down to 2.5 MeV and is flat at lower energies, and normalizing to the ¹²C line fluence, we obtain 99% confidence upper limits of $U_{\rm i} \simeq 4.0 \times 10^{30}$ ergs in accelerated ions. For a spectrum unbroken down to 1 MeV Nucleon⁻¹ that limit becomes $U_i \simeq 4 \times 10^{31}$ ergs; for a low-energy

limit of 0.1 MeV Nucleon⁻¹ the limit is $U_{\rm i} \simeq 1.2 \times 577$ 10^{34} ergs.

5. Energetics of Interplanetary Particles

[40] In addition to the kinetic energy of the CME 580 (section 2) and the energy contained in the thermal plasma 581 and in the accelerated particles that interact in the solar 582 atmosphere (sections 3 and 4), energetic particles that 583 escape from the Sun or are accelerated in interplanetary 584 space represent another significant contribution to the global 585 energy budget. These solar energetic particles (SEPs) can be 586 accelerated at the flare site and/or at shocks driven by the 587 CME and can fill a significant part of the heliosphere. 588 Shock acceleration processes, responsible for a vast major- 589 ity of SEPs, are expected to depend on the strength of the 590 accelerating shock, as well as on the orientation of the shock 591 normal relative to the magnetic field direction. The resulting 592 observed particle spectra in the heliosphere depend strongly 593 on the magnetic connectivity of the observer to the accel- 594 eration site [Cane et al., 1988]. The average heliospheric 595 magnetic field geometry is a Parker spiral, which tends to 596 provide better connections to westerly solar longitudes. 597 However, there are observed large-scale deviations of the 598 magnetic field throughout the heliosphere which makes it 599 very difficult to predict magnetic connectivity. In addition, 600 the particle transport may not be completely field-aligned 601 [Giacalone and Jokipii, 1999], which leads to additional 602 complications.

[41] The 23 July event occurred near the east limb of the 604 Sun (S13E72) and, as is typical for east limb events, was 605 apparently not magnetically well connected to Earth. Near-606 Earth spacecraft such as ACE and GOES did not observe 607 significant energetic particle fluxes that could be traced to 608

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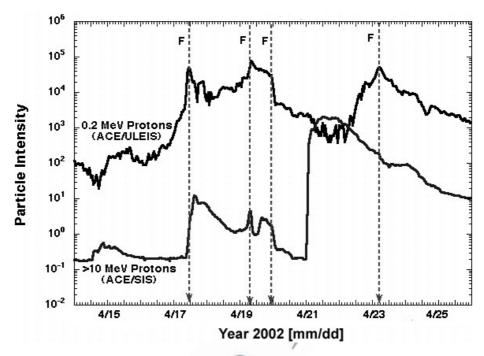


Figure 6. Ion flux as a function of time as measured by ACE/SIS [Stone et al., 1998] and ACE/ULEIS [Mason et al., 1998] for mid-April 2002. The arrival times of forward shocks are indicated.

this event (although interplanetary SEPs from the 23 July event could have been masked by those from an east limb event on 22 July that did produce SEPs at Earth). On the other hand, the 21 April event, at west longitude 84° and south latitude 14° was relatively well connected to Earth, and indeed, a strong interplanetary shock (Mach number $M_A = 3.7$) was observed some 2 days later, at ~ 0415 UT on 23 April. The intensity of 0.2 MeV and >10 MeV protons from 14 April through 26 April is shown in Figure 6. The arrival times of fast forward shocks are also indicated. The intensities of the 0.2 MeV (and to a lesser extent the >10 MeV) peak around the time of shock arrival indicating that acceleration is taking place locally at the shocks.

[42] There is a sharp increase in the >10 MeV proton flux on 21 April within ~25 min of the release of a very fast (\sim 2500 km s⁻¹) CME and an X1.5 flare, indicating a very good magnetic connection. Note that the maximum in the 0.2 MeV proton intensity did not occur until 23 April, more than a day later than these ions would be expected from velocity-dispersion considerations (low-energy ions travel more slowly along field lines than higher-energy ions). It is possible that low-energy ions accelerated close to the Sun were trapped behind the CME-driven shock and did not reach maximum intensity until the shock arrived. This event appears to be a classic example of a gradual event that is dominated by shock-accelerated rather than flareaccelerated particles, as evidenced by its composition (slightly Fe-poor), its time profile, and also the time profile of the associated X-ray flare (see Figure 1).

[43] Figure 7 shows the fluence spectrum (intensity integrated over the period from 21 April to 25 April) for protons, helium, oxygen, neon, and iron. H and He are the most abundant elements in the SEP population, with heavier

ions up though Fe and Ni accelerated to similar energy per 643 nucleon with roughly coronal abundances. The spectra of all 644 ion species appear to consist of two populations: a power 645 law portion at low energies (<5 MeV nucleon⁻¹) that peaks 646 at the time of the shock arrival and exponential spectra at 647 higher energies (e-folding energy ~12 MeV for protons) 648 whose intensity peaks early on 21 April.

[44] Daily electron fluences for the 3 days (21 to 23 April) 650 with the highest intensity are shown in Figure 8, including 651 data from ACE/EPAM (red line) and SAMPEX/PET (blue 652 line). The electron time history (not shown) indicates that 653 most of the electrons were accelerated close to the Sun, with 654 only a small contribution from local acceleration when the 655 shock arrives on 23 April.

[45] It is relatively straightforward to integrate the differ- 657 ential energy spectra in Figures 7 and 8 to obtain the total 658 particle energy incident per cm² at 1 AU. The limits of this 659 integration were taken to be 10 keV (or keV nucleon⁻¹) to 660 infinity. The ion spectra (Figure 7) were extrapolated using 661 the observed power law behavior at low energy and ob- 662 served exponential behavior at high energy. The electron 663 spectra were extrapolated as power laws at both low and 664 high energy (Figure 8). Overall, about 50% of the contri- 665 butions are from ~ 0.1 to 100 MeV nucleon⁻¹ where there 666 are good observations, and the rest are extrapolated. To 667 relate these fluences to the total energy content of energetic 668 particles, it is necessary to take into account that a given 669 particle may have crossed 1 AU several times due to the 670 diffusive nature of the particle propagation so that particles 671 at 1 AU may have multiple opportunities to be counted. 672 Simulations by J. Giacalone (personal communication, 673 2002) [see also Li et al., 2003] using scattering mean free 674 paths of ~0.01 to 1 AU indicate that the probability of 675 crossing 1 AU more than once is energy dependent, with 676

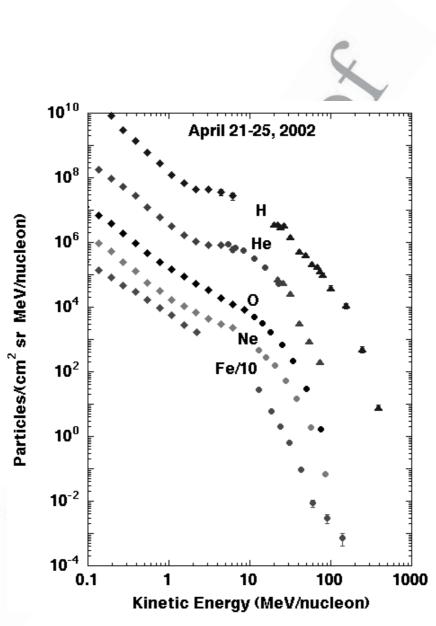


Figure 7. Energy spectra of five species integrated over the period 21-25 April 2002. Included are $2 \le Z \le 26$ measurements from ACE/ULEIS [*Mason et al.*, 1998] and ACE/SIS [*Stone et al.*, 1998] and H and He data (>20 MeV nucleon⁻¹) from SAMPEX/PET [*Cook et al.*, 1993].

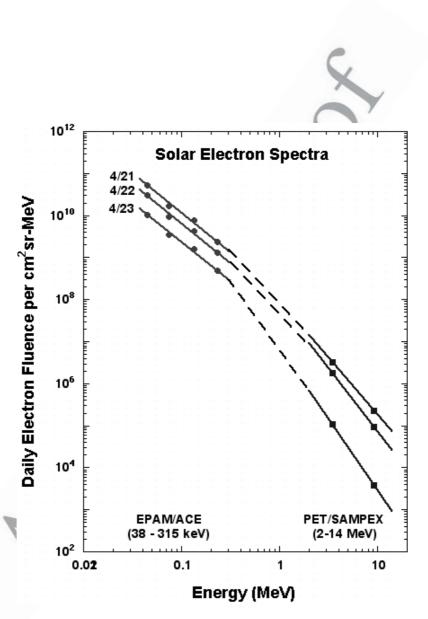


Figure 8. Daily electron fluence measured by ACE/EPAM [*Gold et al.*, 1998] and SAMPEX/PET [*Cook et al.*, 1993] during 21–23 April 2002.

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Table 2. Interplanetary Solar Particle Energy Content by Species

.2	Species	Energy Content, ergs	Fraction of Total	
.3	Protons	2.3×10^{31}	0.817	
.4	Helium	1.8×10^{30}	0.064	
.5	$3 \le Z \le 28$	4.4×10^{29}	0.016	
.6	Electrons	2.9×10^{30}	0.103	
.7	Sum	2.8×10^{31}	1.000	

typical values ranging from ~ 1 crossing at 0.01 MeV, to ~ 3 crossings at 0.1 MeV, to ~ 7 crossings for 10 MeV protons. We have corrected for this probability using a rigidity-dependent, mean-free path adapted from Droege [2001], taking into account the instrument fields of view (e.g., the ACE/SIS and ACE/ULEIS instruments view only in the Sun-facing hemisphere). The result is that because of the multiple crossings, the shock needs to accelerate only about half as many particles as we count in our observations, and the particle energy content needed to produce the observed energy per cm² is reduced by a factor of ~ 2 .

[46] To obtain the total energy contained in interplanetary particles, we must also estimate the surface area through which energetic particles escape. Noting that this shock, apparently centered near W84°, was still accelerating particles when it reached Earth, we obtain a lower limit to this surface area by assuming that the particles are accelerated uniformly on field lines over a solid angle of $\sim \pi$ ster (in other words, assuming that the measured erg/cm² at Earth applies over an area of π AU²).

[47] However, historically, the largest events at 1 AU are those near the central meridian where the nose of the shock passes by Earth (e.g., the 14 July 2000 and 28 October 2003 events from this solar cycle). Indeed, the five largest >10 MeV proton events from 1976 to 2003 (see the NOAA/GOES catalog at http://umbra.nascom.nasa.gov/SEP/seps.html) all originated between E30° and W30° and only one of the top ten is west of W40°. By comparison, the 21 April 2002 event (at W84°) had a near-Earth fluence that was only ~10% of that of the 14 July 2000 and 28 October 2003 central meridian events, although the CME velocities were comparable. This suggests that a correction should be applied to the observed 21 April 2002 fluence to account for its location relative to Earth. We assume a simple model (inspired by the 1997–2003 longitude distribution of >12 MeV O and Si fluences from ACE and the 1976-2003 longitude distribution of >10 MeV proton events from GOES) in which the fluence is a maximum when the CME is launched from the same latitude and longitude as Earth, falling off exponentially with latitude with an e-folding separation of 35° and with longitude with an e-folding separation of 45° for western events and 25° for eastern events. We can then relate the measured fluence at Earth to the total fluence integrated over longitude and latitude. These e-folding separations are similar in magnitude to those obtained by Van Hollebeke et al. [1975], Kahler [1982], and Mason et al. [1984], although with their smaller data sets they did not deduce that the largest events originate near the central meridian. With these corrections, the global intensity of >10 MeV protons (as measured by GOES) in the 21 April 2002 event is \sim 45% of that in the 14 July 2000 event and \sim 29% of that in the 28 October 2003 event. This correction raises the estimated energy content of interplanetary particles in the

21 April 2002 event by a factor of \sim 5 compared with the 730 lower limit estimated above. 731

[48] The total energy content of the interplanetary par- 732 ticles is summarized by species in Table 2, including the 733 corrections for longitude and latitude discussed above. With 734 these corrections, the 21 April event becomes the seventh 735 largest >10 MeV proton event of this solar cycle, and its 736 fluence is now more on a par with that of other large events. Note that the total energy in energetic particles $(2.8 \times 10^{31} \, 738 \, \text{ergs})$ is a significant fraction $(\sim 15\%)$ of the CME kinetic 739 energy $(\sim 1.8 \times 10^{32} \, \text{ergs})$, implying that shock acceleration 740 must be relatively efficient.

[49] By far the largest uncertainty in the energy budget 742 for energetic particles at 1 AU ($U_{\rm p}$ in Table 2) is in the 743 procedure for relating the fluences at Earth to the total 744 interplanetary particle population because of uncertainties in 745 the longitude and latitude intensity distributions. We estimate this uncertainty to be a factor of \sim 3. There is also an 747 uncertainty of $\Delta \log_{10} U_{\rm p} \simeq 0.2$ in the correction for how 748 many times particles cross 1 AU. The relative contribution 749 of the various species are much better known, to perhaps 750 30% for the ions and \sim 50% for electrons. All of these 751 uncertainties are independent, but the overall uncertainty in 752 the energy content of the accelerated interplanetary particles 753 could be as large as a factor of four.

6. Magnetic Energy

[50] The magnetic energy associated with coronal cur- 756 rents is generally considered to be the source of the thermal, 757 kinetic, and radiative energy released in a flare or CME 758 event. This magnetic energy can be expressed as

$$\frac{1}{8\pi} \int_{r>R_0} \left(B^2 - B_p^2\right) dV,\tag{5}$$

where B is the strength of the total magnetic field, B_p is the 761 strength of the potential magnetic field produced by sources 762 below the corona, r is the radial coordinate, and R_0 is the 763 lower boundary of the corona.

[51] Using the MHD virial theorem [Chandrasekhar and 765 Fermi, 1953; Chandrasekhar, 1961; Molodenskii, 1969; 766 Aly, 1984, 1989; Low, 1984, 1999; Litvinenko and Somov, 767 2001], one can express the total magnetic energy in terms of 768 the field components at the lower boundary of the corona as 769

$$\begin{split} U_{\rm B} &= \frac{1}{8\pi} \int_{r>R_0} B^2 dV \\ &= \frac{R_0}{8\pi} \int_{r=R_0} \left(B_r^2 - B_\theta^2 - B_\phi^2 \right) dS - \int_{r=R_0} p \, dS \\ &+ \int_{r>R_0} \left(\frac{\rho G M_0}{r} - 3p \right) dV, \end{split} \tag{6}$$

where B_r , B_θ , and B_ϕ are the spherical components of the 771 total field B, p is the coronal gas pressure, ρ is the coronal 772 density, G is the universal constant of gravitation, M_0 is the 773 solar mass, and dS is the differential surface element. If 774 the gravitational and thermal energy terms are ignored, then 775 the field is force-free, and the magnetic energy available to 776 drive the eruption is given entirely in terms of an integral 777 over the components of the surface field. During the 778 timescale of an eruption the radial component of the 779 magnetic field is essentially constant because of inertial line 780

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Table 3. CME/Flare Energy Budgets for the 21 April 2002 and 23 July 2002 Events

3.2			log ₁₀ (Energy, erg)	
t3.3	Mode	Symbol	21 April 2002	23 July 2002
3.4	Magnetic Flare	$U_{\rm B}$	32.3 ± 0.3	32.3 ± 0.3
t3.5	Thermal plasma, $T > 10 \text{ MK}$	$U_{ m th}$	$31.3^{+0.4}_{-1}$	$31.1^{+0.4}_{-1}$
t3.6	Nonthermal electrons	$U_{\rm e}$	$31.3^{+?}_{-0.5}$	$31.5^{+?}_{-0.5}$
t3.7	Nonthermal ions, >1 MeV nucleon ⁻¹	$U_{\rm i}$	<31.6	31.9 ± 0.5
	CME			
t3.9	Kinetic	U_{K}	32.3 ± 0.3	32.0 ± 0.3
t3.10	Gravitational potential	U_{Φ}	30.7 ± 0.3	31.1 ± 0.3
	Energetic particles at 1 AU	$U_{\mathfrak{p}}$	31.5 ± 0.6	none above
3.11		r		background

tying, which constrains the outward magnetic flux to the same surface area at the photosphere. Therefore if the effects of gas pressure and gravity are negligible, equation (6) implies an upper limit on the total magnetic energy, $U_{\rm B}$, because $(B_{\theta}^2 + B_{\phi}^2)$ must be somewhere in the range between its potential value and zero. For a simple dipole field the upper limit on the total energy set by the virial theorem is twice the potential energy. Other distributions of the surface field tend to give somewhat higher values [see *Wolfson*, 2003].

[52] Owing to the constraints imposed by helicity conservation, not all of the "free" magnetic energy may be available on short timescales to power flares and CMEs; however, it does provide an upper limit on the magnitude of the energy available. If the helicity of the field were known, one could subtract the energy of the equivalent linear force-free field with the same helicity rather than the energy of the potential field as was done above.

[53] Unfortunately, the chromospheric vector magnetic field observations required to apply the magnetic virial theorem are not available for the 21 April and 23 July events. While in principle it is possible to compute the potential field energy from the MDI line-of-sight magnetograms, in practice the active regions which produced the 21 April and 23 July events were too close to the limb for such a calculation. However, other large active regions similar to those involved in the 21 April and 23 July events contain some 10³³ ergs in nonpotential (free) magnetic energy [Metcalf et al., 1995, 2002]. For example, in AR 7216 analyzed by Metcalf et al. [1995], the free magnetic energy is $U_{\rm B} = (1.2 \pm 0.2) \times 10^{33}$ ergs, which is about one third of the total magnetic energy in AR7216 ($U_{\rm B}$ = (3.2 ± 0.2) \times 10³³ ergs). A free energy of 10³³ ergs is some 5 times the total energy budget of the 21 April and 23 July events, demonstrating that the conversion of roughly 20% of the available free energy is required to power these events.

7. Putting it All Together: Energy Partition in the Two Events

[54] Table 3 shows the combined results of the previous sections, in the form $\log_{10}U \pm \Delta\log_{10}U$, for each energy component. Figure 9 shows the summary results for the 23 July event in pictorial form.

[55] We should note at the outset that the uncertainties in all the measured quantities are large. For example, as pointed out in section 4, the energy in accelerated ions is

uncertain by several orders of magnitude because of the 825 unknown lower limit to the accelerated ion spectrum (we 826 show results for a lower limit of 1 MeV in Table 3). Also, 827 not all these energy contents are independent: for example, 828 the energy in nonthermal electrons is converted through 829 Coulomb collisions into energy in the thermal plasma. 830 Hence one should not simply sum these individual components up to get a "total" energy for the event.

[56] Notwithstanding these remarks, however, a few 833 (cautious) remarks can still be made. First, it is clear that 834 in both events the coronal mass ejection has the dominant 835 component of the released energy, and furthermore, it 836 contains a substantial fraction (30%) of the available mag- 837 netic energy. Second, the energy in accelerated electrons is 838 comparable to that in accelerated ions. Third, at least for the 839 low-energy spectral cutoffs used herein, both electron and 840 ion energies are a half to a whole order of magnitude 841 smaller than the energy contained in the CME. Fourth, the 842 peak energy in the thermal soft X-ray plasma is about an 843 order of magnitude less than the energy in the accelerated 844 (electrons + ions above 1 MeV); the rest of the energy 845 deposited by these particles is presumably converted into 846 radiation in other wavebands (e.g., EUV, optical) (cf. 847 Canfield et al. [1980] for estimates) and into kinetic energy, 848 perhaps of the CME itself. Fifth and finally, the energy in 849 interplanetary particles accelerated by the CME shock in the 850 21 April event is some 15% of the energy in the CME itself, 851 an indication of the acceleration efficiency of the interplan- 852

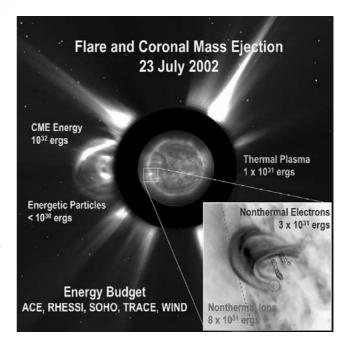


Figure 9. Summary of the morphology and energetics of the 23 July event. The main frame shows the coronal mass ejection structure in LASCO, together with an EIT 195 Å image of the Sun. The expanded region at the lower right shows the hard X-ray (50–100 keV) contours, the centroid of the 2.223 MeV line emission (circle), and the postflare loops as observed by TRACE. The best estimates for the energies of the various components are indicated directly on the figure. See color version of this figure at back of this issue.

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- etary shock. We encourage the development of theoretical 853 854 estimates against which to assess this result.
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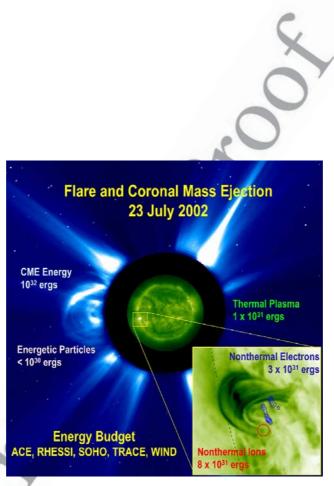


Figure 9. Summary of the morphology and energetics of the 23 July event. The main frame shows the coronal mass ejection structure in LASCO, together with an EIT 195 Å image of the Sun. The expanded region at the lower right shows the hard X-ray (50-100 keV) contours, the centroid of the 2.223 MeV line emission (circle), and the postflare loops as observed by TRACE. The best estimates for the energies of the various components are indicated directly on the figure.